Factor the sum and difference of cubes.

1. $x^{3}+27$
2. $64 y^{3}-27$
3. $32 x^{6}-500 x^{3}$
4. $f(x)=x^{3}+3 x^{2}-6 x-8$
A. What are all of the possible rational zeros of $f(x)$ ?
B. Determine all of the rational roots. Show work.

| Solve each. |
| :--- |
| $5 . x^{2}-4 x+4=0$ $6 . x^{2}-81=0$ $7 . x^{2}+x-12=0$ <br> $8 . x^{3}-5 x^{2}-4 x+20=0$ $9.2 x^{2}+13 x-24=0$ $10.6 x^{2}-31 x+5=0$ <br> $11.4 x+12+x^{2}+3 x=0$ $12 . x^{3}+5 x^{2}-9 x-45=0$ $13 . x^{2}-8 x-48=0$ |

Multiple Choice Select the best choice for each problem.
14. Find all of the rational zeros of $g(x)=2 x^{3}+4 x^{2}-2 x-4$.
A) $x=\{2,4,-2,-4\}$
B) $x=\{-2,1,2\}$
C) $x=\{4,1,-4\}$
D) $x=\{-4,-1,4\}$
E) $x=\{-2,-1,1\}$
15. Consider $g(x)=2 x^{3}+4 x^{2}-2 x-8$.

If we were to list all of the possible rational zeros using the rational root theorem ( $p / q$ ) for the polynomial we would have how many possible rational zeros?
A) 3
B) 4
C) 5
D) 8
E) more than 8

Find all zeros and list any multiplicity.
16. $y=x^{3}(x-2)(x+4)^{2}$
17. $y=x(x+2)^{2}(x+3)$
18. $y=x^{4}+7 x^{3}+12 x^{2}$

Find all the zeros of the function using synthetic division, factoring or quadratic formula.
Find $p / q$ 's.
19. $f(x)=2 x^{3}+3 x^{2}-59 x-30$
20. $f(x)=x^{3}-5 x^{2}-48 x+108$
21. $f(x)=10 x^{4}-13 x^{3}-21 x^{2}+10 x+8$

