

Name: _____ Date: _____

Solving Exponential Functions

Solve each equation:

1. $3^{2x-5} = 3^{x+3}$

$$2x-5 = x+3$$

$$x-5 = 3$$

$$\boxed{x=8}$$

2. $9^{x-5} = 27$

$$3^{2(x-5)} = 3^3$$

$$2(x-5) = 3$$

$$2x-10 = 3$$

$$2x = 13$$

$$\boxed{x = \frac{13}{2}}$$

3. $5^{2x+3} = 625$

4. $81^{x+3} = \left(\frac{1}{3}\right)^{5x-6}$

$$81^{x+3} = 3^{-1(5x-6)}$$

$$3^{4(x+3)} = 3^{-1(5x-6)}$$

$$4x+12 = -5x+6$$

$$9x+12 = 6$$

$$9x = -6$$

$$\boxed{x = -2/3}$$

5. $\left(\frac{1}{3}\right)^x - 9 = 18$

$$\left(\frac{1}{3}\right)^x = 27$$

$$3^{-1(x)} = 27$$

$$3^{-1x} = 3^3$$

$$-1x = 3$$

$$\boxed{x = -3}$$

6. $4^x = \left(\frac{1}{2}\right)^{x-3}$

7. $8^x = 1$

8. $4^x + 5 = 21$

9. $16^{2x+4} = \left(\frac{1}{4}\right)^{x-8}$

Write in simplest radical form. (Using only one radical sign in each problem)

10. $64^{1/2}$

11. $8^{-1/2}$

12. $a^{3/5} \cdot a^{1/5}$

13. $(4x^2y)^{1/3}$

$$a^{3/5+1/5} = a^{4/5}$$

$$\boxed{\sqrt[5]{a^4}}$$

$$\boxed{\sqrt[3]{4x^2y}}$$

Write each expression with fractional exponents.

14. $\sqrt{8x^4}$

15. $3a\sqrt[6]{a^4}$

16. $xy^3\sqrt[4]{5xy}$

17. $\sqrt{x^3y^6}$

$$xy^3 \cdot 5^{1/4} x^{1/4} y^{1/4}$$

$$\boxed{5^{1/4} x^{5/4} y^{13/4}}$$

Simplify. (Radical Form)

18. $2x \cdot y^{4/5} z^{1/5}$

19. $(xy^2)^{1/3}$

20. $(x^{-1/2} \cdot x^{3/4})^{-2}$

$$21. \frac{x^{4/5}}{3x^{2/5}} = x^{4/5-2/5} = x^{2/5}$$

$$\frac{x^{2/5}}{3} = \frac{\sqrt[5]{x^2}}{3}$$

22. $(2x^{1/2}y^{3/4})(3x^{1/4}) =$

$$6x^{1/2+1/4}y^{3/4} = 6x^{3/4}y^{3/4}$$

$$= \boxed{6\sqrt[4]{x^3y^3}}$$

23. $2x^{5/7}y^{3/7} =$

24. $6(a^2b^3)^{1/8} =$

25. $(2a^4b^{3/10})^2 =$

26. $(5a^{-1/2}b^{-3/2})^2 =$

28. $\left(\frac{2x^3y^{1/2}}{x^2}\right)^{-1} =$

29. $(4x^3y^5)^{1/6} =$