

Ex: Divide and simplify if needed:

$$10) \frac{\sqrt[3]{32}}{\sqrt[3]{-4}} = \sqrt[3]{\frac{32}{-4}} = \sqrt[3]{-8}$$

$\begin{matrix} 2 & 4 \\ & 2 \end{matrix}$

$\boxed{-2}$

$$11) \frac{\sqrt[3]{162x^5}}{\sqrt[3]{3x^2}} = \sqrt[3]{\frac{162x^5}{3x^2}} = \sqrt[3]{54x^3}$$

$\begin{matrix} 2 & 3 & 3 \\ & 3 & 3 \end{matrix}$

$\boxed{3x\sqrt[3]{2}}$

$$12) \frac{\sqrt{12x^4}}{\sqrt{3x}} = \sqrt{\frac{12x^4}{3x}} = \sqrt{4x^3}$$

$\begin{matrix} 2 & 2 \\ & 2 \end{matrix}$

$\boxed{2x\sqrt{x}}$

Ex: Rationalize the denominator:

$$14) \frac{\sqrt{3x^5}}{\sqrt{5y}} \cdot \frac{\sqrt{5y}}{\sqrt{5y}} = \frac{\sqrt{15x^5y}}{\sqrt{25y^2}}$$

$\begin{matrix} 5 & 5 \\ & 5 \end{matrix}$

$\boxed{\frac{x^2\sqrt{15yx}}{5y}}$

$$15) \frac{\sqrt{2x^3}}{\sqrt{10xy}} = \sqrt{\frac{2x^3}{10xy}} = \sqrt{\frac{1x^2}{5y}}$$

$\begin{matrix} 2 & 2 \\ & 2 \end{matrix}$

$\frac{\sqrt{x^2}}{\sqrt{5y}} = \frac{x \cdot \sqrt{5y}}{\sqrt{5y} \cdot \sqrt{5y}}$

$\begin{matrix} 5 & 5 \\ & 5 \end{matrix}$

$\boxed{\frac{x\sqrt{5y}}{5y}}$

$$16) \frac{\sqrt{3a}}{\sqrt{9b^2c}} = \frac{\sqrt{3a}}{3b\sqrt{c}} \cdot \frac{\sqrt{c}}{\sqrt{c}} = \frac{\sqrt{3ac}}{3b\sqrt{c^2}}$$

$\begin{matrix} 3 & 3 \\ & 3 \end{matrix}$

$\boxed{\frac{\sqrt{3ac}}{3bc}}$

$$17) \frac{\sqrt{x}}{\sqrt{8y}} = \frac{\sqrt{x}}{\sqrt{8y}} \cdot \frac{\sqrt{8y}}{\sqrt{8y}} = \frac{\sqrt{8xy}}{\sqrt{64y^2}}$$

$\begin{matrix} 2 & 4 \\ & 2 \end{matrix}$

$\begin{matrix} 8 & 8 \\ & 8 \end{matrix}$

$\boxed{\frac{\sqrt{2xy}}{4y}}$

$$18) \frac{8\sqrt{30x^3}}{4\sqrt{24x}} = \frac{2\sqrt{5x^2} \cdot \sqrt{6}}{\sqrt{6} \cdot \sqrt{6}} = \frac{2\sqrt{30x^2}}{\sqrt{36}} = \frac{2x\sqrt{30}}{6}$$

$\begin{matrix} 2 & 2 & 2 \\ & 2 & 2 \end{matrix}$

$\boxed{\frac{x\sqrt{30}}{3}}$

To rationalize the denominator:
Conjugate of $a + \sqrt{b} = a - \sqrt{b}$

Ex: $(\sqrt{5} + \sqrt{2})(\sqrt{5} - \sqrt{2})$

$\begin{matrix} 2 & 2 \\ & 2 \end{matrix}$

$\boxed{5 - 2 = 3}$

First & Last

Ex: Rationalize the denominator.

$$19) \frac{5}{2 + \sqrt{3}} \cdot \frac{(2 - \sqrt{3})}{(2 - \sqrt{3})} = \frac{10 - 5\sqrt{3}}{4 - \sqrt{9}} = \frac{10 - 5\sqrt{3}}{4 - 3} = \boxed{10 - 5\sqrt{3}}$$

$$20) \frac{2 - \sqrt{3}}{4 + \sqrt{3}} \cdot \frac{(4 - \sqrt{3})}{(4 - \sqrt{3})} = \frac{8 - 2\sqrt{3} - 4\sqrt{3} + 3}{16 - 3} = \frac{11 - 6\sqrt{3}}{13}$$

21) A rectangle has an area of 120 units². If one side is $5\sqrt{2}$ units, what is the measure of the remaining side length?

$A = lw$

$120 = 5\sqrt{2}w$

$\frac{120}{5\sqrt{2}} = \frac{w}{\sqrt{2}}$

$\frac{120 \cdot \sqrt{2}}{5\sqrt{2} \cdot \sqrt{2}} = w$

$\frac{120\sqrt{2}}{5\sqrt{4}} = w$

$\frac{120\sqrt{2}}{10} = w$

$\boxed{12\sqrt{2} = w}$